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## $B V g^{\prime} r^{\prime}$ CCD Observations of AS Cas

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1665 magnitude measurements in the $B, V, g^{\prime}$, and $r^{\prime}$ filters were acquired for the double-mode Cepheid AS Cas. The light curves for both fundamental and first-overtone modes were constructed.

We performed CCD observations of the Cepheid AS Cas in October 2020-February 2021 (the JD range 2459126-2459265) at the Caucasus Mountain Observatory (CMO, Russia) with the $60-\mathrm{cm}$ telescope using the Andor iKon-L camera, $2048 \times 2048$ pixels, with a pixel size of 13.5 microns. The Johnson $B V$-band filters and $g^{\prime} r^{\prime}$-band filters of the ZTF survey system (Masci et al., 2019) were used. Information about the CMO and description of the observing data reduction technique can be found in our previous paper (Berdnikov et al., 2020). We obtained a total of 1665 magnitude measurements with photometric errors close to 0.01 mag .

Observations are available in a text file in the html version of the paper (Table 1). The light curves, constructed with the fundamental period, are shown in Fig. 1.

Using the Period04 code (Lenz and Breger, 2004), we determined the frequencies for the fundamental, $F_{0}$, and first-overtone, $F_{1}$, modes. Then we used 17 combinations of these frequencies (Table 2; amplitudes in filter $B$ are given for information) to approximate our observations by Fourier series. For this purpose, we converted all observations to intensities and, for each $i$ th observation, set up conditional equations in the form:

$$
\begin{equation*}
I_{i}=I_{0}+\sum\left[\left(A_{j} \cdot \sin \left(2 \pi t_{i} F_{j}\right)+B_{j} \cdot \cos \left(2 \pi t_{i} F_{j}\right)\right], \quad j=1-17,\right. \tag{1}
\end{equation*}
$$

where $I_{i}$ is the observed intensity; $I_{0}$ is the mean intensity; $A_{j}$ and $B_{j}$ are the amplitudes; $t_{i}$ is the Julian Date of observation; $F_{j}$ is the frequency. The system of linear equations (1) is solved by the least-squares method for unknowns $I_{0}, A_{j}$, and $B_{j}$.

Clearly, the difference between observed intensity, $I_{i}$, and the sum (1) without harmonics of any particular mode gives us the intensity for this mode. These intensities, converted back to magnitudes, form the light curves of AS Cas for the fundamental and first-overtone modes given in Table 3 and Table 4 (in the html version of the paper), respectively. They are shown in Fig. 2 and Fig. 3, constructed with the light elements:

$$
\begin{equation*}
\text { Max HJD }=2448874.8469+3^{\mathrm{d}} 024089443 \cdot E \tag{2}
\end{equation*}
$$

and

$$
\begin{equation*}
\text { Max HJD }=2448875.1768+2.155014317 \cdot E, \tag{3}
\end{equation*}
$$

respectively for the fundamental and first-overtone modes.


Figure 1. $B g^{\prime} V r^{\prime}$ observations (Table 1) phased with the fundamental period.
Table 2. Frequencies for equations (1). Amplitudes for the filter $B$ are given

| Name of frequency | Frequency, $\mathrm{d}^{-1}$ | Amplitude, mag |
| :---: | :---: | :---: |
| $F_{0}$ | 0.33067805 | 0.3366 |
| $2 F_{0}$ | 0.66135610 | 0.0961 |
| $3 F_{0}$ | 0.99203415 | 0.0361 |
| $4 F_{0}$ | 1.32271220 | 0.0062 |
| $F_{0}+F_{1}$ | 0.79471209 | 0.1209 |
| $2 F_{0}+F_{1}$ | 1.12539014 | 0.0723 |
| $F_{1}-F_{0}$ | 0.13335599 | 0.0686 |
| $F_{0}+2 F_{1}$ | 1.25874613 | 0.0421 |
| $2\left(F_{0}+F_{1}\right)$ | 1.58942418 | 0.0288 |
| $2 F_{0}-F_{1}$ | 0.19732206 | 0.0143 |
| $3 F_{1}+F_{0}$ | 1.72278017 | 0.0127 |
| $3 F_{0}-F_{1}$ | 0.52800011 | 0.0080 |
| $2\left(F_{1}-F_{0}\right)$ | 0.26671198 | 0.0022 |
| $F_{1}$ | 0.46403404 | 0.2197 |
| $2 F_{1}$ | 0.92806808 | 0.0414 |
| $3 F_{1}$ | 1.39210212 | 0.0079 |
| $4 F_{1}$ | 1.85613616 | 0.0054 |

The sum (1) for harmonics of any particular mode gives the template light curve for this mode; these are shown in Fig. 4 and Fig. 5 (for the fundamental and first-overtone modes, respectively) and presented in the html version of the paper as Table 5 and Table 6, which list the $B, g^{\prime}, V$, and $r^{\prime}$-band magnitudes for phases from 0 to 0.995 with a step


Figure 2. Fundamental-mode light curves of AS Cas.
of 0.005 . We plan to use these templates to study the behavior of pulsating periods of AS Cas.

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## References:

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Figure 3. First-overtone light curves of AS Cas.


Figure 4. Fundamental-mode template curves of AS Cas.


Figure 5. First-overtone template curves of AS Cas.

